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M. C. Thompson, Jr. , H. B. Janes, L. E. Wood, &  
Dean Smith



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Phase and Amplitude Scintillations of Microwave  
Signals Over an Elevated Atmospheric Path  
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10 May 1971

PHASE AND AMPLITUDE SCINTILLATIONS OF MICROWAVE  
SIGNALS OVER AN ELEVATED ATMOSPHERIC PATH

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Background

A technique has been proposed to obtain global surveys of atmospheric density profiles by means of a set of co-orbital earth satellites [Lusignan, et al., 1969]. The method involves measurements of phase delays in microwave signals propagated between pairs of satellites, so arranged that the signal passes through the atmosphere along a part of its path.

A basic factor in the success of this technique is the influence of random atmospheric variability (turbulence) on signal phase and amplitude. These signal properties are also involved in the bandwidth required in the satellite terminal equipment. In addition, other atmospheric propagation effects, notably fading, could have a significant effect on the overall effectiveness of the system. The phenomenon of principal concern in this respect is the very deep (e. g., > 50 dB) fades associated with certain types of refractive index gradients known to occur.

The objectives of the experiment reported here were:

1. to obtain a basic statistical description of phase and fading characteristics using a fixed propagation path chosen to simulate certain



aspects of the satellite-to-satellite configuration; and,

2. in conjunction with the fixed path measurements, to obtain simultaneous measurements of atmospheric index structure near the propagation path.

### Location

Since only the portions of the atmosphere above about 2.5 km are to be probed in the proposed system, a path was sought with two high terminals and a maximum surface clearance. Chiefly because of logistic factors (e.g., roads, shelter, power, etc.) the path selected was between Mt. Haleakala, Maui, Hawaii, and Mauna Loa, Hawaii. The terminal elevations are 3025 m and 3300 m, respectively, and the path length is 150 km.

Figures 1 and 2 show the locations and profile, including the half-power beam widths of the antennas.

### Radio Measurements

Three converging paths were instrumented at frequencies near 10 GHz. A single terminal at Mauna Loa Observatory was equipped with a 2-m diameter parabolic dish having a  $1.2^\circ$  beam width. The Haleakala terminal was equipped with three 1.25-m diameter dishes having  $1.8^\circ$  beams. These antennas were spaced along a line perpendicular to the nominal direction of propagation with 10 m between the first and second, and 100 m between the first and third. This permitted

measurement of the variability of phase-front orientation.

The quantities recorded were:

1. Amplitudes of signals from each of the three antennas with a dynamic range of from 20 to 50 dB, precision of 0.5 dB, and frequency response from 0 to 30 Hz.
2. Phase variability on each of the three paths with unlimited dynamic range, 0.5 degree resolution (at the X-band frequency), and response from 0 to 30 Hz.
3. Phase differences between the 10 m spaced antennas and between the 100 m pair, with same recording ranges, etc., as in (2). A description of the phase measurement system is given in Appendix IV (attached).

#### Atmospheric Measurements

A Piper "Aztec" aircraft was equipped with a microwave refractometer and flown in the vicinity of the path to obtain refractive index structure and statistics. Because of the locations of the beam intersections (Fig. 2), flights were concentrated between about 2 and 4 km elevation.

#### Operations and Results

The radio signals were observed continuously from 0800 hours June 15 through 0500 hours June 29. Aircraft flights were made on 23 occasions during this period.

During the first four days of the run signal amplitudes were generally variable but without the characteristic "V"-shaped appearance associated with the very deep fades. In the next four days the deep fades occurred a large fraction of the time. Figure 3 shows an example of these two types of activity.

Initially, the plan was to obtain index profiles at two locations along the path plus a record of horizontal index variability along the path; the latter data would provide estimates of the index structure parameter  $C_n$  which might correlate with signal variability [Tatarski, 1961; Porcello, 1970].

At the onset of deep fading, it was decided to modify the flight plan to obtain as many vertical sections (profiles) as feasible along the path. These would show the horizontal extent of the vertical index features that might be related to the deep fading.

As an approximate preliminary description of the fading, the data have been divided into four groups in terms of the amplitude variability within 30-min periods.

The groups are defined as follows:

- Type A: < 5 dB peak to peak fading range.
- Type B: > 5 dB peak to peak fading range.
- Type C: > 5 dB with from 1 to 5 "V"-shaped fades of > 15 dB.
- Type D: > 5 dB with over 5 "V"-shaped fades > 15 dB.

This classification is used in Figs. 4 and 5, together with the corresponding flight patterns, to summarize the amplitude variability with respect to time and time of day.

Figures 6, 7, and 8 show examples of index profiles obtained during Flights 4 and 12, the same periods used for the fading samples in Fig. 3. Two kinds of profiles were obtained from the refractometer data. The "low-pass" output of the refractometer was used to produce the familiar profiles of  $N$  versus height. At the same time, a "band-pass" output provides a profile of small-scale  $N$  variability as a function of height. Both low-pass and band-pass profiles are shown for Flight 4 in Fig. 6. They are plotted separately for Flight 12 in Figs. 7 and 8. Because of the relatively low angle at which the plane ascends and descends (about  $6^\circ$ ), the record is subject to horizontal index variations to an appreciable degree. Thus one should not assume that the resulting plots represent the true vertical structure of index.

A description and the results of the analysis of the refractometer data from level flights along the propagation path is given in Appendix I (attached). The results consist of values of the refractive index structure parameter,  $C_n$ , computed from level flight segments. A complete

set of refractive index profile graphs is included as a part of this report in separate Appendix II.

### Signal Data Analysis

From the 14-day measurement period, detailed statistical analysis was performed on a sample of signal phase, phase difference, and amplitude data taken from each of the 23 aircraft flight periods. (In the results, note that "sample number" and "flight number" are synonymous, and that there was no flight 6.)

Each of the signal data samples is 40 min in length except for 7 samples which were shortened to avoid phase discontinuities. The discontinuities were caused by deep fading in 5 cases and by equipment trouble in the other 2 cases. Frequent fading discontinuities precluded statistical analysis of the phase data from samples 8, 11, and 12.

With the exceptions noted above, each signal sample was analyzed to produce the cumulative distribution and power spectrum of each of the phase and amplitude variables, and cross-correlation and coherency functions of appropriate pairs of variables. The original analog magnetic tape recordings were digitized at the rate of 12.5 points per variable per second. Of these, every tenth point was used (without smoothing) in the cross-correlation computations. For the power spectrum and coherency computations, the data were smoothed by averaging non-overlapping groups of 10 points in order to minimize aliasing effects. The



cumulative distributions were also computed from smoothed data.

The results of the signal data analyses are included as a part of this report in separate Appendix III. They consist of the following:

1. Computer printouts of:

a. Cumulative distributions of phase and amplitude data at each of the 3 antenna locations on Haleakala, and of 2 phase-difference records (from the 10-m path separation of antennas 1, 2, and the 100-m separation of antennas 1, 3). These include histograms, standard deviations, 10%, 50%, and 90% levels and (for amplitude) the mean level.

b. Cross-correlation functions of the phase data for 10 and 100 meter path separations, and of the corresponding amplitude data.

c. Power spectra and coherency functions for the same data mentioned in b above, and power spectra of the two phase-difference variables.

Examples of the computer tabulations are given in Figs. 9 through 11.

2. Computer-generated graphs of:

a. Power spectra of phase, phase difference, and amplitude.

b. Coherency functions of phase and amplitude.

c. Cumulative distributions of amplitude.

Examples are given in Figs. 12 through 16.

With regard to units, the amplitude data are expressed in terms



of decibels relative to an arbitrary reference level common to all the samples recorded on a given path. Thus it is possible to compare amplitude levels from sample to sample on the same path (as is done in the amplitude distribution graphs), but amplitude levels on different paths should not be compared.

The phase data are all expressed in phase degrees at 9.6 GHz. Because phase continuity was not maintained from sample to sample, the phase levels listed in the distributions are simply relative to the sample mean.

These restrictions on comparisons of phase and amplitude levels do not, of course, apply to comparisons of phase and amplitude variability and covariability (i. e. , standard deviation, interdecile range, cross-correlation coefficient, power spectral density, and coherency). The only caution here would be with regard to the amplitude on path 2, which was recorded with a detector having a smaller dynamic range than those used on paths 1 and 3. Hence, the amplitude variability statistics from path 2 are less accurate than those from the other two paths.

#### Acknowledgment

We gratefully acknowledge the contributions of the following persons and organizations whose assistance made this work possible: At the

Haleakala terminal, the facilities of the University of Hawaii Observatory were made available through the courtesy of Dr. John Jeffries, Director, Geophysical Institute. The other terminal was located at the Mauna Loa Observatory of the ESSA Environmental Research Laboratories, operated by the Atmospheric Physics and Chemistry Laboratory, Dr. H. Weickmann, Director.

## List of Figures

1. Map of propagation path.
2. Path profile.
3. Samples of fading data.
4. Summary of flight schedule and types of signal fading.
5. Distribution of flight periods and fading types versus time of day.
6. Index and index variability profiles, Flight 4.
7. Index profiles, Flight 12.
8. Index variability profiles, Flight 12.
9. Distribution printout with histogram.
10. Cross-correlation printout with plot.
11. Spectra and coherency printout.
12. Cumulative distribution of amplitude, Flights 1 - 4.
13. Amplitude spectra, Flight 4.
14. Phase spectra, Flight 4.
15. Amplitude coherency, Flight 12.
16. Phase coherency, Flight 4.

## References

1. Lusignan, B. , G. Madrell, A. Morrison, J. Pomalaza, and S. Unger, "Sensing the earth's atmosphere with occultation satellites," Proc. IEEE 57, No. 4, April 1969.
2. Thompson, M. C. , Jr. , and M. J. Vetter, "Single path phase measuring system for three-centimeter radio waves," Rev. Sci. Instr. 29, No. 2, Feb. 1958.
3. Tatarski, V. L. , Wave Propagation in a Turbulent Medium, McGraw-Hill Book Co. , Inc. , New York, 1961.
4. Porcello, L. J. , "Turbulence-induced phase errors in synthetic-aperture radars, IEEE Trans. Aerospace Electron. Sys. AES-6, No. 5, Sept. 1970.





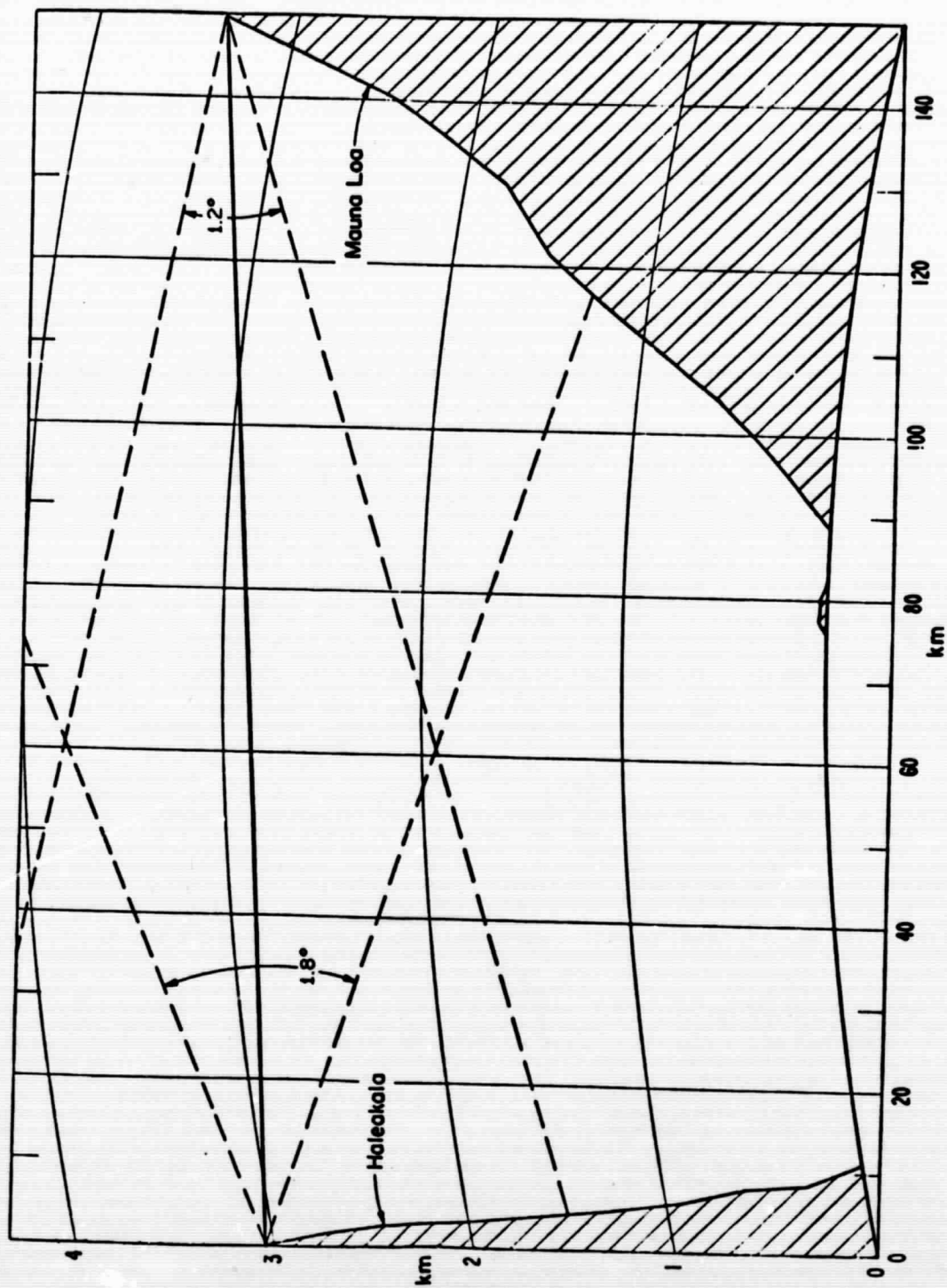


Fig. 2. Vertical profile of propagation path. The dashed lines indicate the half-power beamwidth of the antennas.



# SIGNAL FADING ON SIMULATED SATELLITE OCCULTATION PATH

## Horizontal Antenna Separation at Haleakala: 100 m

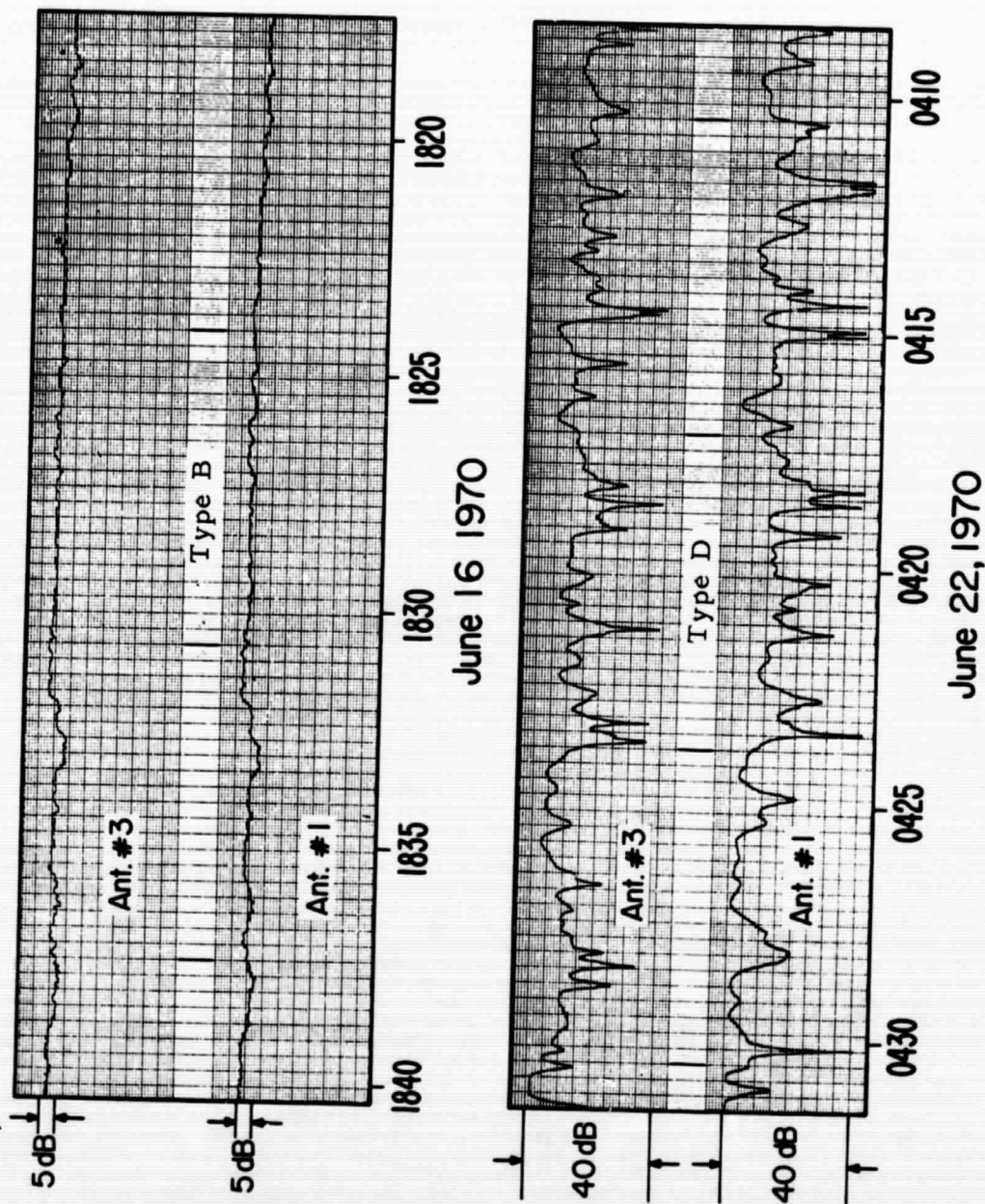


Fig. 3

# SUMMARY OF FADING DATA HAWAII, JUNE 1970 9.6 GHz

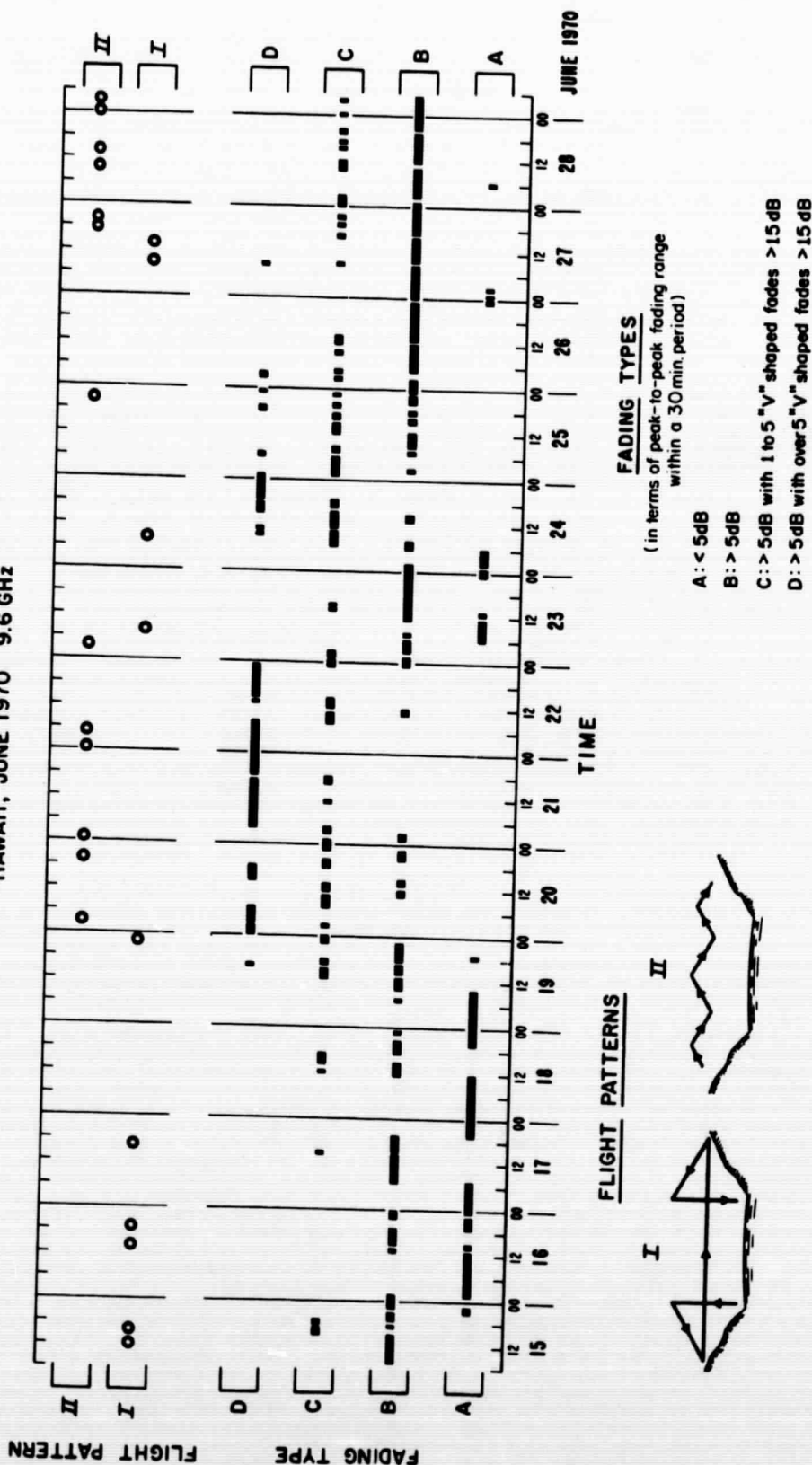


Fig. 4.

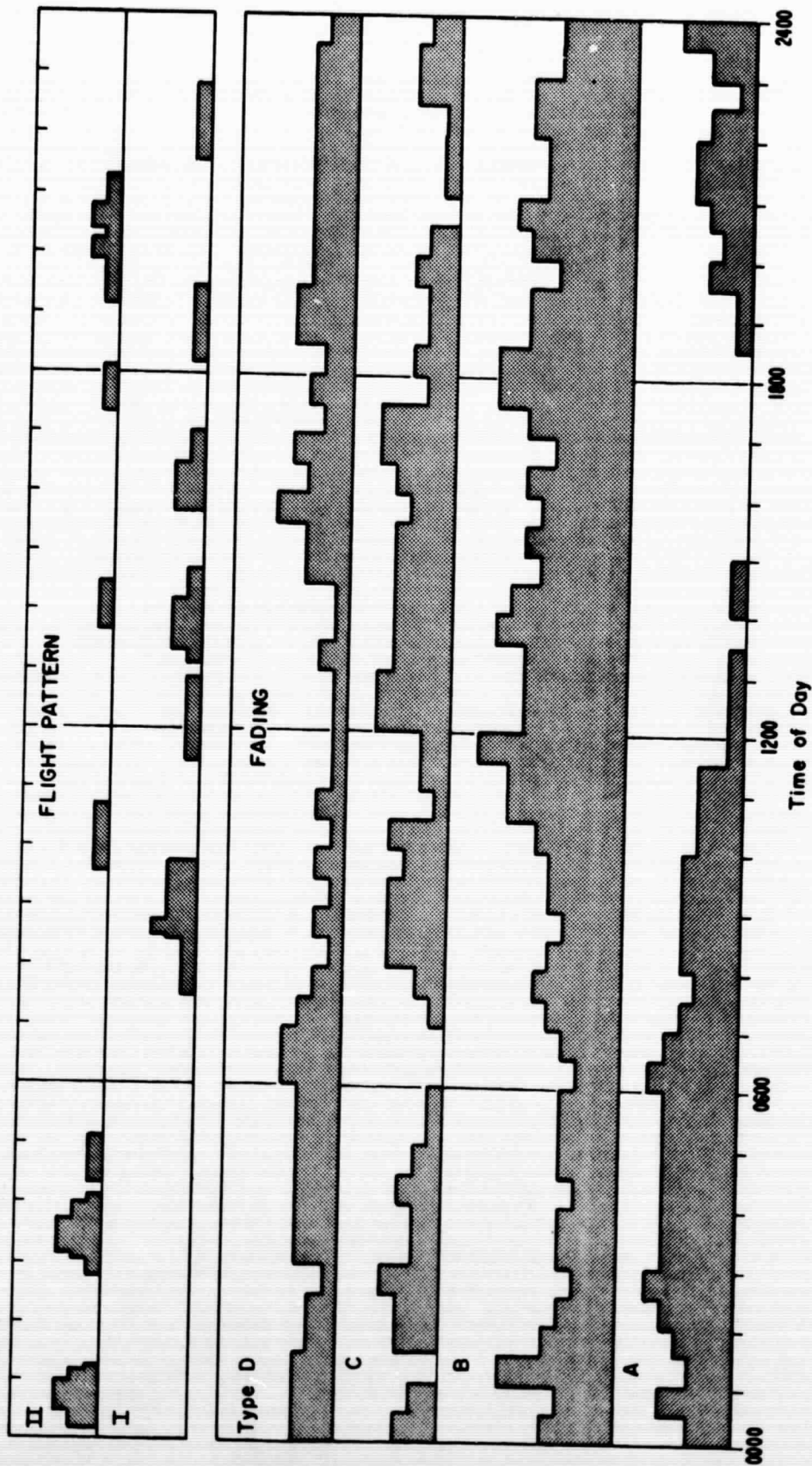


Fig. 5. Distribution of fading occurrences and refractometer flights with time of day. See Fig. 4 for explanation of fading types and flight patterns.

FLIGHT 4    HAWAII  
1811 - 1924    June 16, 1970

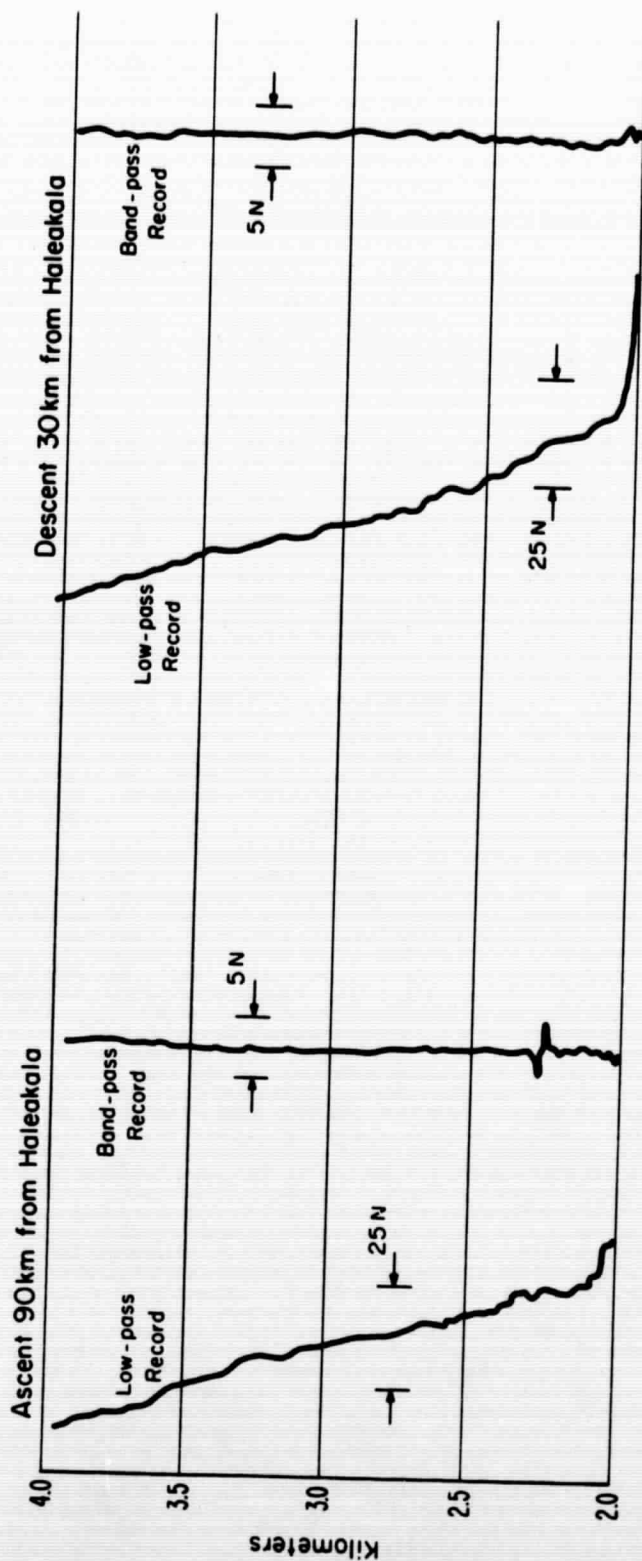


Fig. 6. Examples of refractive index profile data. Profiles from both low-pass and band-pass recordings are shown for Flight 4.

FLIGHT 12 HAWAII  
0407 - 0453 June 22, 1970

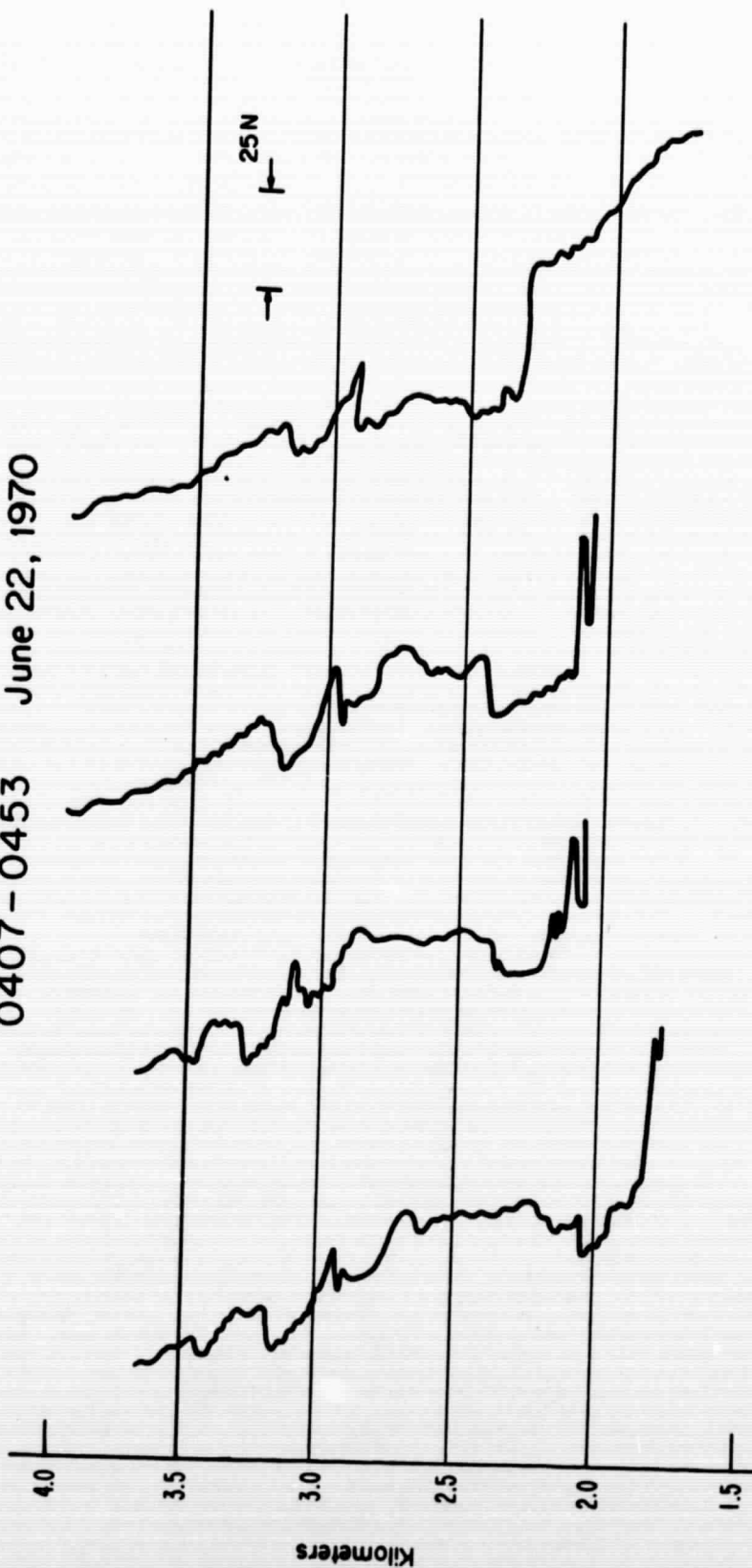


Fig. 7. Example of refractive index profile data. Four profiles from low-pass recordings made during Flight 12.

FLIGHT 12 HAWAII  
0407-0453 June 22, 1970

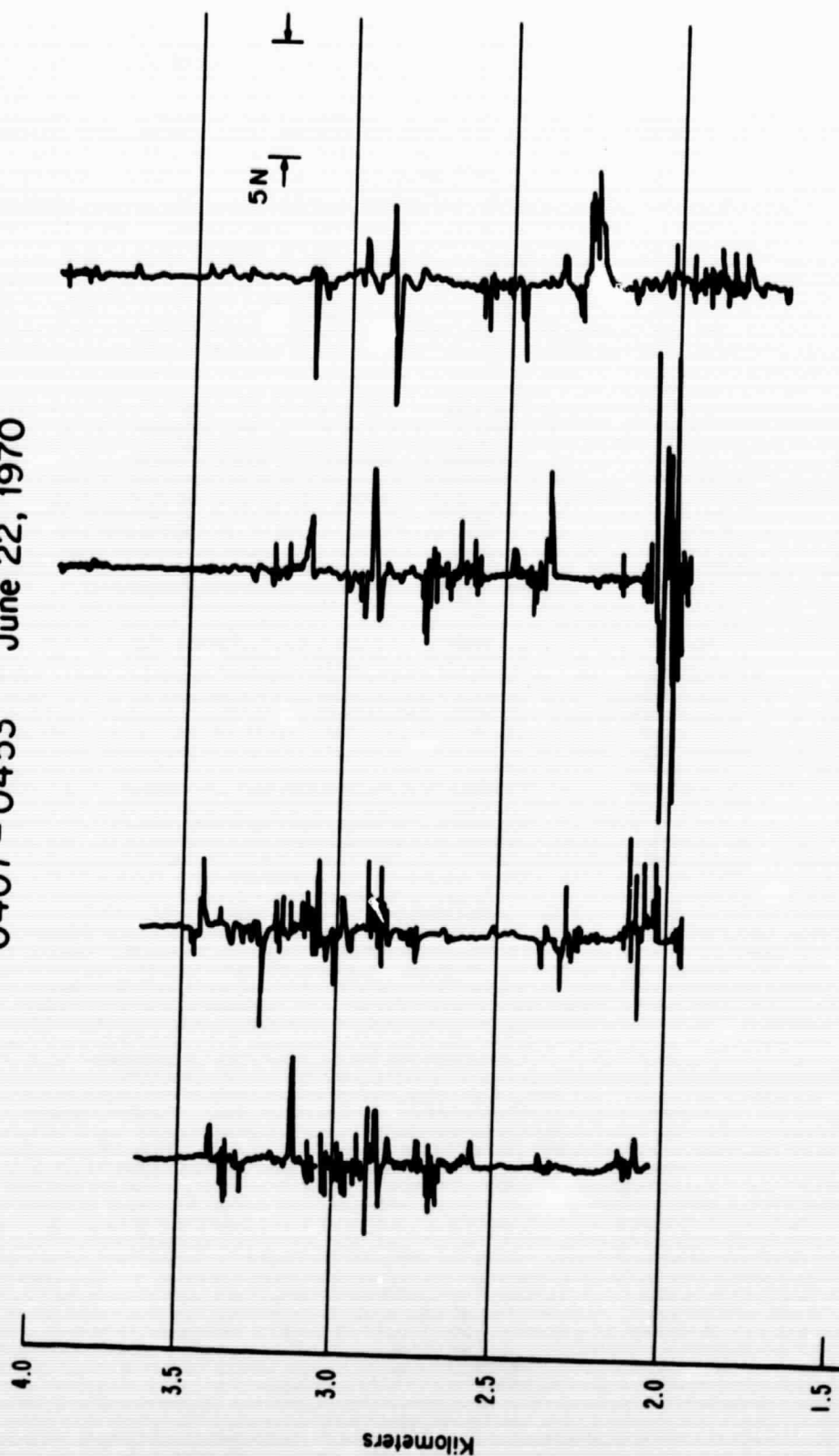


Fig. 8. Example of refractive index profile data. Four profiles from band-pass recordings made during Flight 12.



OCCULTATION EXPERIMENT  
 VARIABLE: = AMPLITUDE AT ANTENNA 1  
 DISTRIBUTION ANALYSIS  
 DATA COUNT = 3044  
 SAMPLE NO. 4  
 TIME: 1840 - 1920 JUNE 16, 1970  
 UNITS: DECIBELS  
 SAMPLING INTERVAL 0.8 SECONDS

LEVEL	DISTRIBUTION COUNT	PERCENT ≥ LEVEL	PERCENT AT LEVEL	50
3.52+001	0	0.0		
3.47+001	12	0.4	X	
3.43+001	46	1.9	X	
3.38+001	74	4.3	XXX	
3.33+001	86	7.2	XXXX	
3.28+001	183	13.2	XXXXXXXX	
3.23+001	237	21.0	XXXXXXXXXX	
3.18+001	252	29.2	XXXXXXXXXX	
3.13+001	259	37.7	XXXXXXXXXX	
3.09+001	305	47.8	XXXXXXXXXX	
3.04+001	339	58.9	XXXXXXXXXX	
2.99+001	312	69.2	XXXXXXXXXX	
2.94+001	358	80.9	XXXXXXXXXX	
2.89+001	275	89.9	XXXXXXXXXX	
2.84+001	118	93.8	XXXXX	
2.79+001	92	96.8	XXXX	
2.75+001	66	99.0	XXX	
2.70+001	26	99.9	XX	
2.65+001	3	103.0	X	
2.60+001	1	100.0	X	

MEAN: 3.086+001  
 STANDARD DEVIATION: 1.619+010  
 10 X LEVEL: 3.31+001  
 50 X LEVEL: 3.08+001  
 90 X LEVEL: 2.89+001

(LEVELS SHOWN ABOVE ARE RELATIVE TO AN ARBITRARY REFERENCE COMPON TO ALL SAMPLES OF THIS VARIABLE)

HEADER IN 12040 3511 70000

Fig. 9. Example of signal amplitude distribution analysis included in separate Appendix III.

	FREQUENCY	COHERENCY	M(F) OF X	M(F) OF Y	FREQUENCY	COHERENCY	M(F) OF X	M(F) OF Y
1	6.250-003	0.051-001	5.610-001	5.203-001	51	3.100-001	4.716-001	4.795-002
2	1.250-002	0.051-001	1.806-001	1.776-001	52	3.250-001	4.798-001	4.695-002
3	1.075-002	0.161-001	9.020-000	7.986-000	53	3.313-001	3.698-001	4.605-002
4	2.500-002	7.772-001	4.956-001	3.927-000	54	3.375-001	3.446-001	4.466-002
5	3.125-002	7.591-001	3.691-000	2.693-000	55	3.438-001	4.065-001	4.701-002
6	3.750-002	7.658-001	1.951-000	1.811-000	56	3.500-001	4.719-001	4.903-002
7	4.375-002	7.873-001	1.381-000	1.336-000	57	3.563-001	5.068-001	4.794-002
8	5.000-002	8.088-001	1.228-000	1.054-000	58	3.625-001	4.784-001	4.363-002
9	5.625-002	7.726-001	1.095-000	9.060-001	59	3.688-001	4.125-001	4.433-002
10	6.250-002	6.713-001	8.945-001	8.668-001	60	3.750-001	4.172-001	5.121-002
11	6.875-002	5.907-001	7.765-001	8.011-001	61	3.813-001	4.259-001	5.517-002
12	7.500-002	6.461-001	7.806-001	7.944-001	62	3.875-001	3.715-001	5.573-002
13	8.125-002	7.571-001	5.900-001	6.317-001	63	3.938-001	3.301-001	5.781-002
14	8.750-002	8.154-001	5.373-001	5.683-001	64	4.000-001	4.117-001	5.985-002
15	9.375-002	8.250-001	5.615-001	6.025-001	65	4.063-001	5.155-001	5.651-002
16	1.000-001	7.964-001	5.672-001	5.772-001	66	4.125-001	5.587-001	5.961-002
17	1.063-001	7.641-001	4.745-001	4.872-001	67	4.188-001	6.487-001	7.182-002
18	1.125-001	7.508-001	4.127-001	4.250-001	68	4.250-001	5.773-001	7.182-002
19	1.188-001	7.644-001	3.677-001	3.677-001	69	4.313-001	4.373-001	5.617-002
20	1.250-001	7.569-001	3.509-001	3.602-001	70	4.375-001	3.647-001	4.425-002
21	1.313-001	6.990-001	3.751-001	3.977-001	71	4.438-001	3.116-001	4.004-002
22	1.375-001	6.011-001	3.740-001	4.011-001	72	4.500-001	4.021-001	4.955-002
23	1.438-001	5.604-001	3.703-001	3.611-001	73	4.563-001	5.210-001	7.611-002
24	1.500-001	6.501-001	2.861-001	3.033-001	74	4.625-001	5.901-001	6.077-002
25	1.563-001	7.825-001	2.631-001	2.561-001	75	4.688-001	6.082-001	7.648-002
26	1.625-001	6.793-001	2.649-001	2.793-001	76	4.750-001	5.042-001	6.159-002
27	1.688-001	6.633-001	2.378-001	2.735-001	77	4.813-001	6.321-001	6.629-002
28	1.750-001	6.821-001	2.208-001	2.210-001	78	4.875-001	7.459-001	8.086-002
29	1.813-001	7.171-001	2.135-001	2.280-001	79	4.938-001	7.480-001	1.022-002
30	1.875-001	7.341-001	2.240-001	2.139-001	80	5.000-001	6.978-001	6.220-002
31	1.938-001	7.261-001	2.130-001	1.072-001	81	5.063-001	4.919-001	5.675-002
32	2.000-001	6.722-001	1.700-001	1.561-001	82	5.125-001	3.159-001	5.016-002
33	2.063-001	6.051-001	1.627-001	1.520-001	83	5.188-001	2.309-001	4.063-002
34	2.125-001	5.694-001	1.591-001	1.551-001	84	5.250-001	2.233-001	4.276-002
35	2.188-001	5.765-001	1.401-001	1.426-001	85	5.313-001	2.558-001	3.607-002
36	2.250-001	5.975-001	1.402-001	1.301-001	86	5.375-001	2.915-001	3.617-002
37	2.313-001	5.225-001	1.326-001	1.120-001	87	5.438-001	3.331-001	6.105-002
38	2.375-001	3.674-001	1.233-001	0.420-002	88	5.500-001	6.495-001	4.086-002
39	2.438-001	2.153-001	1.103-001	6.614-002	89	5.563-001	6.938-001	6.915-002
40	2.500-001	1.353-001	1.155-001	6.444-002	90	5.625-001	6.282-001	5.013-002
41	2.563-001	9.059-002	1.136-001	7.251-002	91	5.688-001	0.078-001	7.003-002
42	2.625-001	1.804-001	1.161-001	7.600-002	92	5.750-001	3.945-001	5.004-002
43	2.688-001	1.153-001	1.102-001	6.936-002	93	5.813-001	3.948-001	3.966-002
44	2.750-001	9.331-002	9.964-002	6.821-002	94	5.875-001	3.956-001	6.113-002
45	2.813-001	1.395-001	0.795-002	5.611-002	95	5.938-001	3.719-001	3.975-002
46	2.875-001	1.903-001	7.411-002	5.095-002	96	6.000-001	4.210-001	3.407-002
47	2.938-001	2.265-001	6.800-002	4.230-002	97	6.063-001	5.002-001	3.479-002
48	3.000-001	2.644-001	6.072-002	4.027-002	98	6.125-001	6.641-001	6.252-002
49	3.063-001	2.950-001	5.167-002	4.144-002	99	6.188-001	6.617-001	4.283-002
50	3.125-001	3.710-001	4.717-002	3.913-002	100	6.250-001	6.114-001	3.900-002

Fig. 11. Example of cross-spectrum analysis of signal amplitude data included in separate Appendix III.

MAXIMUM CORRELATION AT A POSITIVE LAG MEANS VARIATIONS OCCURRED FIRST AT X.

PLOT SYMBOLS: + (-) MEANS CORRELATION COEFFICIENTS FOR POSITIVE (NEGATIVE) LAG  
 0 MEANS BOTH COEFFICIENTS ARE APPROXIMATELY EQUAL

THESE ANSWERS ARE FROM ORIGINAL DATA SPACED BY 10 POINTS  
 VARIANCE (X) = 3.04744+000 VARIANCE (Y) = 2.60894+000 COVARIANCE = 2.90220+000

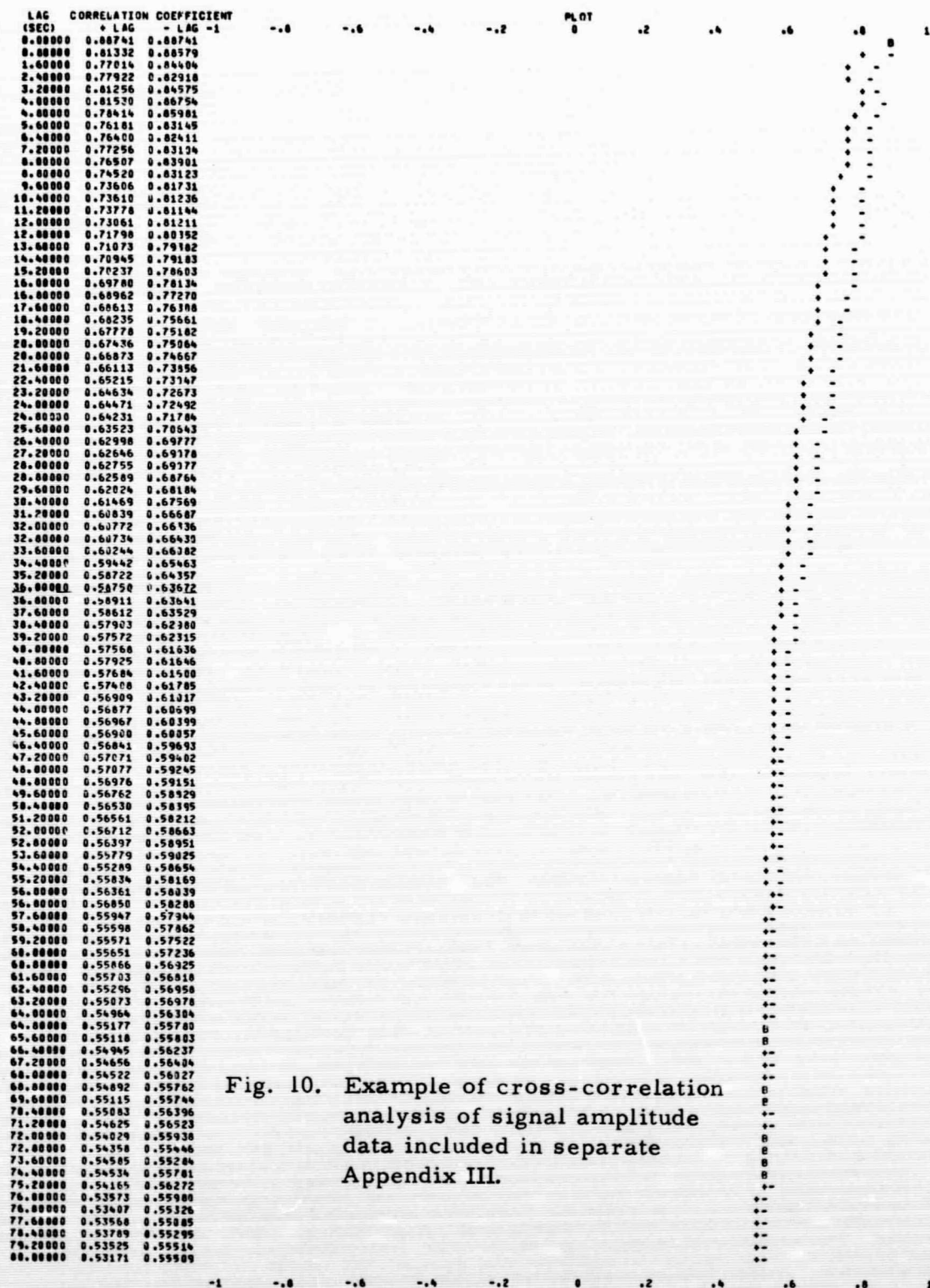


Fig. 10. Example of cross-correlation analysis of signal amplitude data included in separate Appendix III.

# OCCULTATION EXPERIMENT

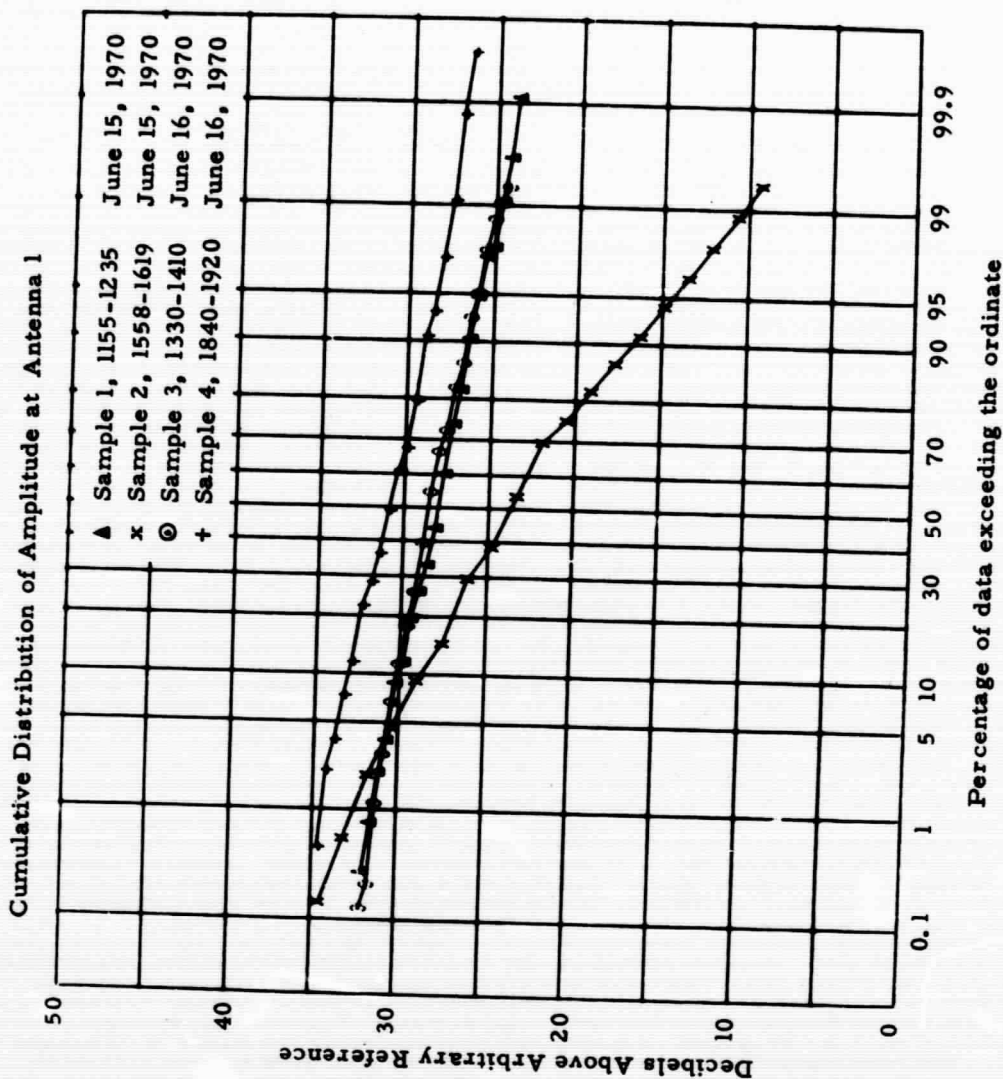


Fig. 12

# OCCULTATION EXPERIMENT

Amplitude Power Spectra, Sample 4, 1840-1920, 6/16/70

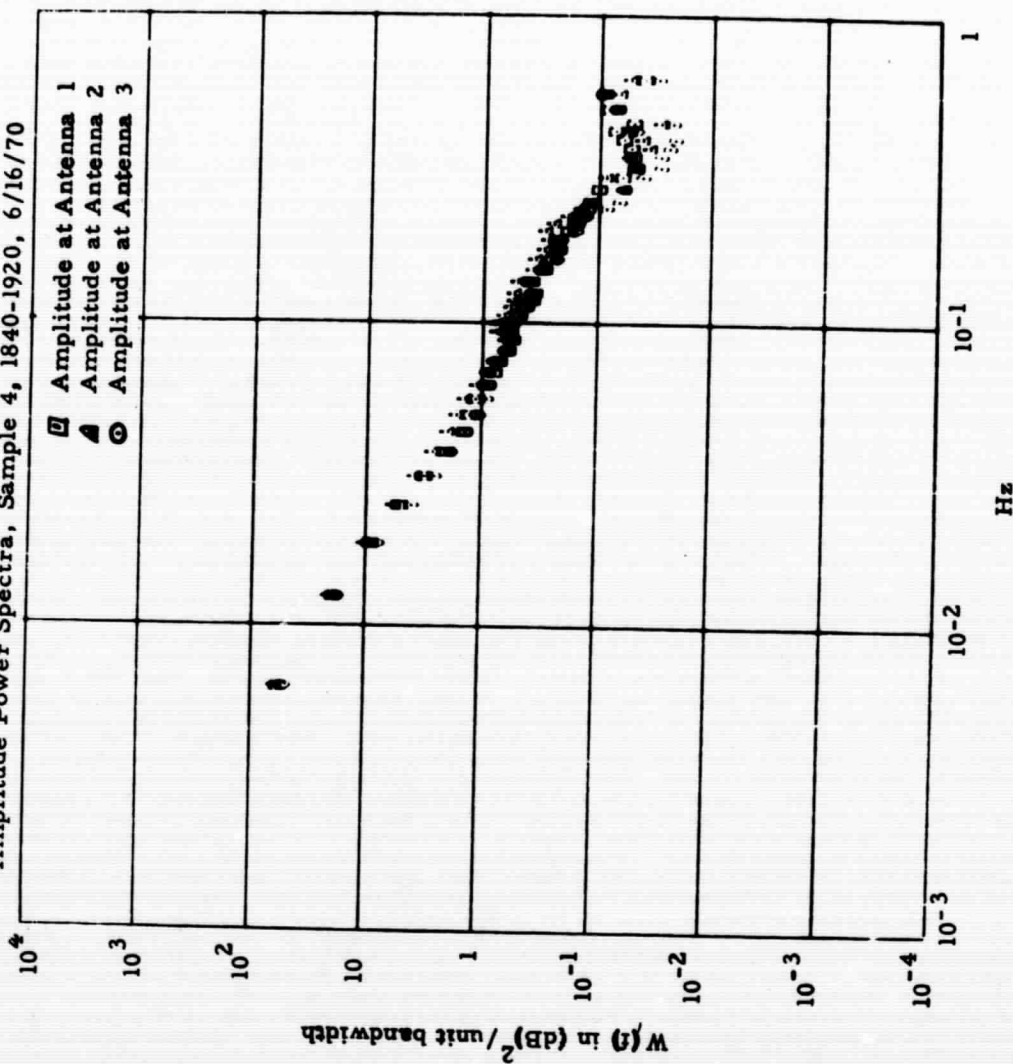


Fig. 13



# OCCULTATION EXPERIMENT

Phase Power Spectra, Sample 4, 1840-1920, June 16, 1970

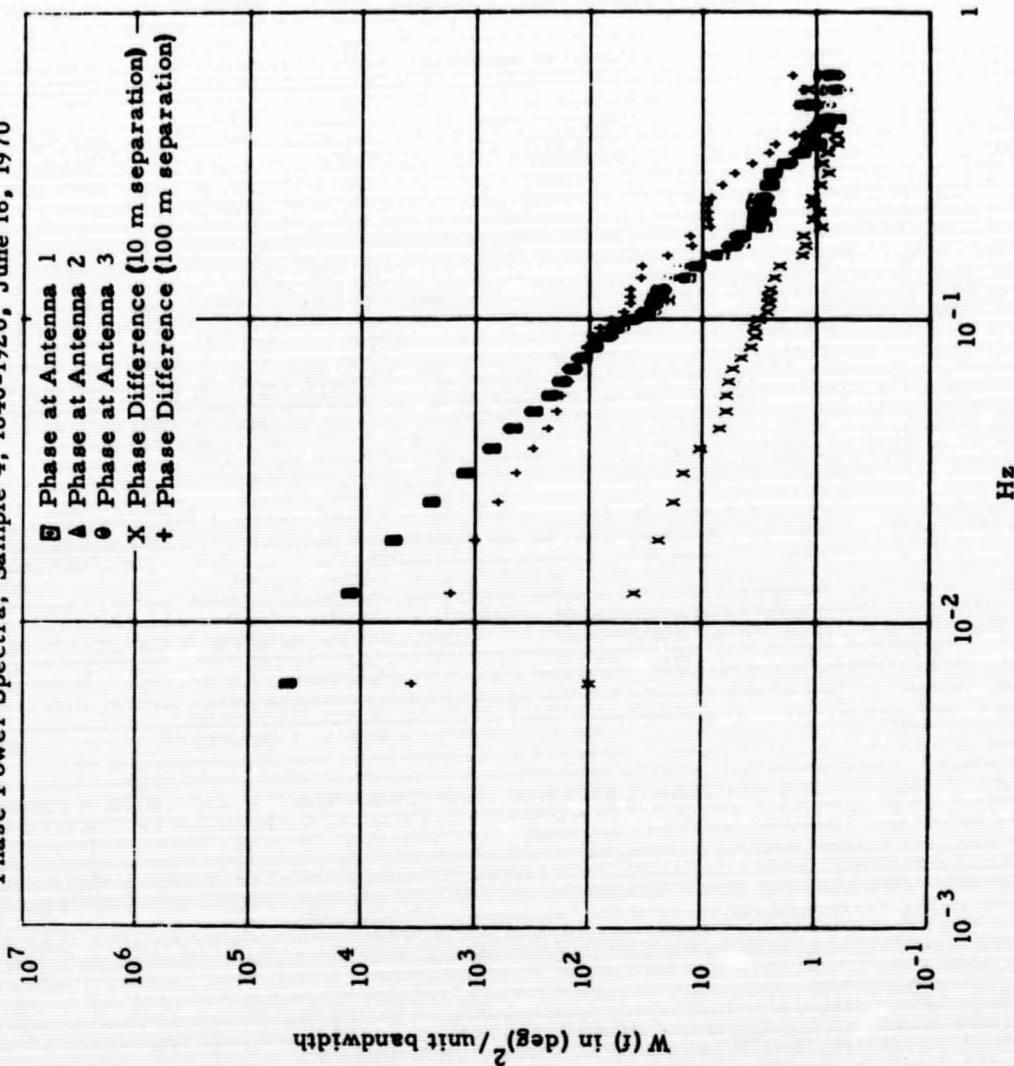


Fig. 14



# OCCULTATION EXPERIMENT

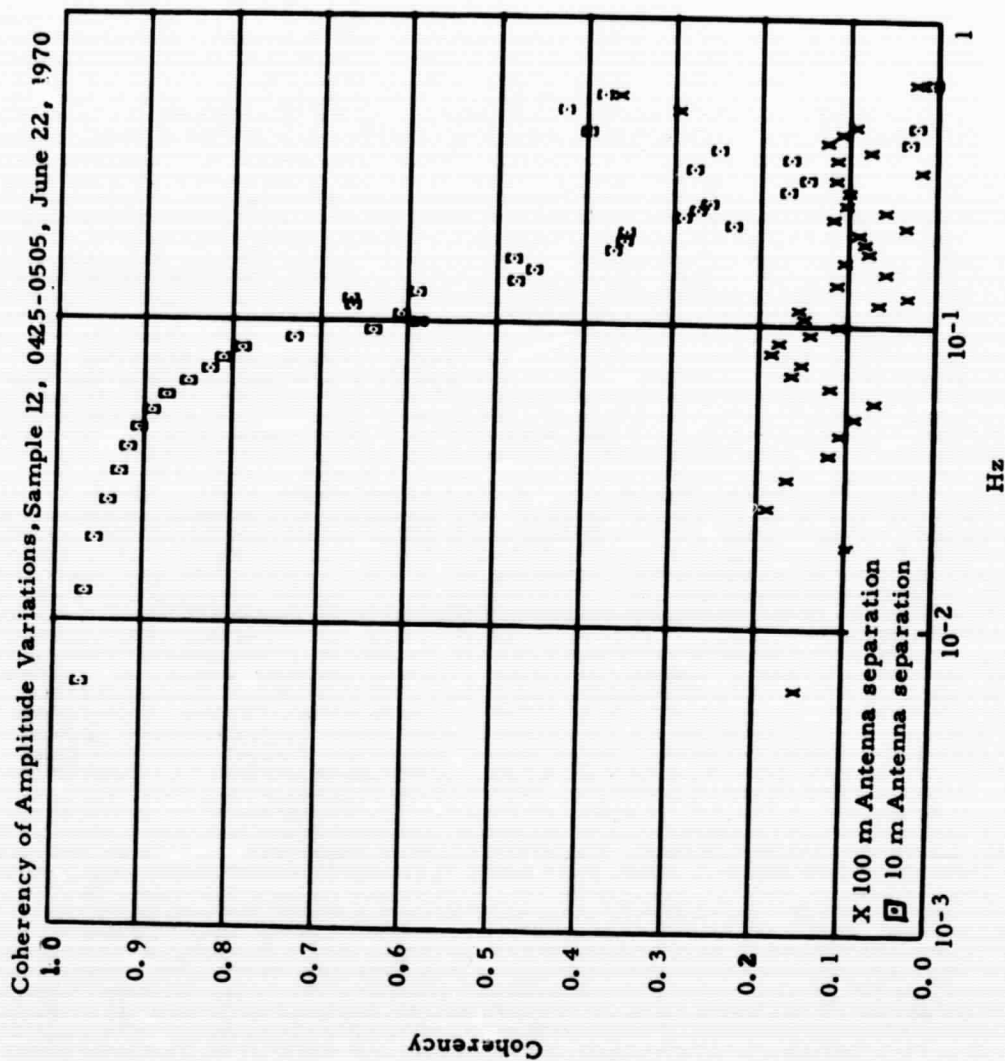


Fig. 15

# OCCULTATION EXPERIMENT

Coherency of Phase Variations, Sample 4, 1840-1910, June 16, 1970

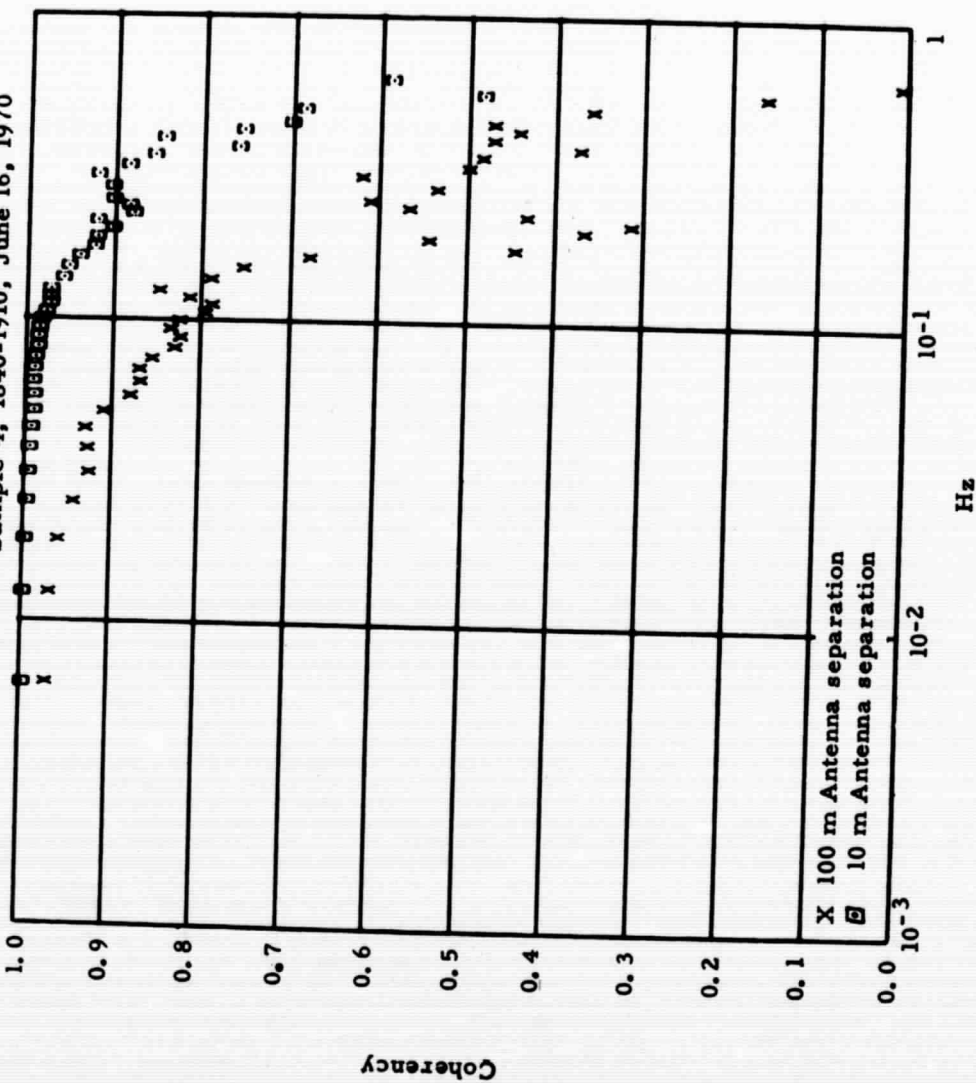


Fig. 16

## Appendix I

### Estimation of the refractive index structure parameter $C_n^2$

One of the objectives of this experiment was to obtain estimates of the atmospheric refractive index structure parameter  $C_n^2$  along the propagation path in conjunction with the phase and amplitude variability measurements. This was accomplished during 10 of the sample periods in which flight pattern type I was flown. (See sketch in Fig. 4.)

Three estimates of  $C_n^2$  were obtained from the level portion of each flight. Each  $C_n^2$  value was computed from a 3-minute segment taken from the continuous magnetic tape record of refractive index variations. Briefly, the steps in the computation were as follows:

1. The continuous analog tape record was digitized at the rate of 800 points per second.
2. The power spectrum was computed over the frequency range 0.04 to 40 Hz, which is the pass band of the high-resolution output of the refractometer. The high frequency end of the spectrum was contaminated by intrusion of the system noise spectrum, so that the effective frequency range of the analysis was from 0.04 Hz to an upper limit that varied from about 0.2 to 20 Hz, depending on the signal-to-noise ratio of the data.
3. The structure function,  $D(r)$ , was computed from each power spectrum and the corresponding aircraft airspeed data for  $r$  (spatial separation of refractive index points) ranging from 10 m to 1 km.

4.  $C_n^2$  was then computed as the slope of a linear regression of  $D(r)$  on  $r^{2/3}$ , in line with the defining equation:

$$D(r) = C_n^2 r^{2/3}.$$

The  $C_n^2$  values are tabulated below. The data segments from each flight are identified as "A", "B", or "C". Segments "A" were taken near the northern, or Haleakala, end of the path; segments "B" were taken near the middle of the path, and segments "C" were taken near the southern, or Mauna Loa, end.

Flight No.Segment

	<u>A</u>	<u>B</u>	<u>C</u>
1	$2.74 \times 10^{-15} \text{ m}^{-2/3}$	$1.14 \times 10^{-15} \text{ m}^{-2/3}$	$2.76 \times 10^{-15} \text{ m}^{-2/3}$
2	$1.08 \times 10^{-15}$	$3.21 \times 10^{-15}$	$1.90 \times 10^{-14}$
3	$3.24 \times 10^{-16}$	$5.45 \times 10^{-15}$	$1.59 \times 10^{-15}$
4	$2.82 \times 10^{-15}$	$8.57 \times 10^{-16}$	$2.29 \times 10^{-16}$
5	--	$1.37 \times 10^{-15}$	$4.81 \times 10^{-15}$
7	$6.67 \times 10^{-15}$	$2.78 \times 10^{-14}$	$1.11 \times 10^{-13}$
14	$7.41 \times 10^{-16}$	$4.60 \times 10^{-15}$	$1.75 \times 10^{-14}$
15	$1.39 \times 10^{-13}$	$1.00 \times 10^{-14}$	$7.27 \times 10^{-16}$
17	$2.27 \times 10^{-14}$	$9.66 \times 10^{-15}$	$4.52 \times 10^{-15}$
18	$7.04 \times 10^{-14}$	$4.74 \times 10^{-14}$	$7.82 \times 10^{-14}$



## APPENDIX IV

### Method of Measuring Phase, Phase Difference, and Amplitude

The phase measurements were made using a technique developed by Thompson and Vetter [1] and shown in Fig. 1.

At the left terminal, a stable microwave signal is generated at frequency  $f$ . This signal is fed to the antenna through a circulator which also couples a small amount of power to the mixer to serve as the local oscillator to heterodyne the small signal received from the opposite terminal.

At the right terminal, a second microwave signal is generated and phase locked below the frequency of the small signal received from the left terminal by an amount  $\delta_1$ . Most of this power is transmitted back over the path with a small fraction being used as local oscillator for the right-hand mixer.

The two mixers thus produce signals with frequencies and phases respectively (left and right)

$$\delta_1, \left[ \phi_0 - \phi_1 - \frac{n_1 L}{c} (f - \delta_1) \right],$$

$$\delta_1, \left[ \phi_0 - \phi_1 + \frac{n_1 L f}{c} \right],$$

where  $n_1$  is the average refractive index along path 1 (length  $L$ ), and  $\phi_0$  and  $\phi_1$  are reference phases for the two microwave signals.

The left-hand IF is telemetered to the right terminal where its phase is

$$\phi_0 - \phi_1 = \frac{n_1 L}{c} (f - \delta_1) + \frac{n_1 L}{c} \delta_1 .$$

This signal and the local IF are compared in a phase recorder and give an output of

$$\alpha_1 = \frac{2 n_1 L f}{c} - \frac{2 n_1 L \delta_1}{c} .$$

Since

$$\delta \approx f \times 10^{-5} , \quad \frac{\alpha_1}{2} \doteq \theta_1 \equiv \frac{n_1 L f}{c} ,$$

the phase shift over path 1.

This process is repeated at antennas 2 and 3 using different frequency offsets between the right-hand signal and the left-hand signal to provide different IF's. Each pair of IF's is processed the same way as described above to obtain the three path phase records,  $\theta_1$ ,  $\theta_2$ , and  $\theta_3$ , separately.

To minimize the errors in determining the phase differences between paths, the six IF signals (3 pairs) are combined as shown in Fig. 2.

Lower side band mixers are used to combine X with Y and X' with Y'. The result is two second IF's having frequency phases (with  $\delta_2 > \delta_1$ ),

$$D: (\delta_2 - \delta_1), \left[ \phi_1 - \phi_2 - \frac{Lf}{c} (n_1 - n_2) \right]$$

$$D': (\delta_2 - \delta_1), \left[ \phi_1 - \phi_2 + \frac{Lf}{c} (n_1 - n_2) - \frac{L}{c} (n_1 \delta_1 - n_2 \delta_2) \right] .$$

Comparing these signals in a phase recorder gives

$$\beta_{12} = \frac{2Lf}{c} (n_1 - n_2) + \frac{L}{c} (n_2 \delta_2 - n_1 \delta_1) .$$

Since  $n_2 \approx n_1$  and  $(\delta_2 - \delta_1) \ll f$ , we have

$$\frac{\beta_{12}}{2} \approx (\theta_1 - \theta_2) \equiv \Delta\theta_{12} .$$

By repeating this process with X, Z and X', Z', we obtain a record of  $\Delta\theta_{13}$ .

Amplitudes for all paths are recorded in terms of the IF signals at the right-hand terminals using commercial amplitude detectors.

### Reference

- [1] Thompson, M. C., Jr., and M. J. Vetter (1958), "Single path measuring system for three-centimeter radio waves," Rev. Sci. Instr. 29, No. 2, 148-150.

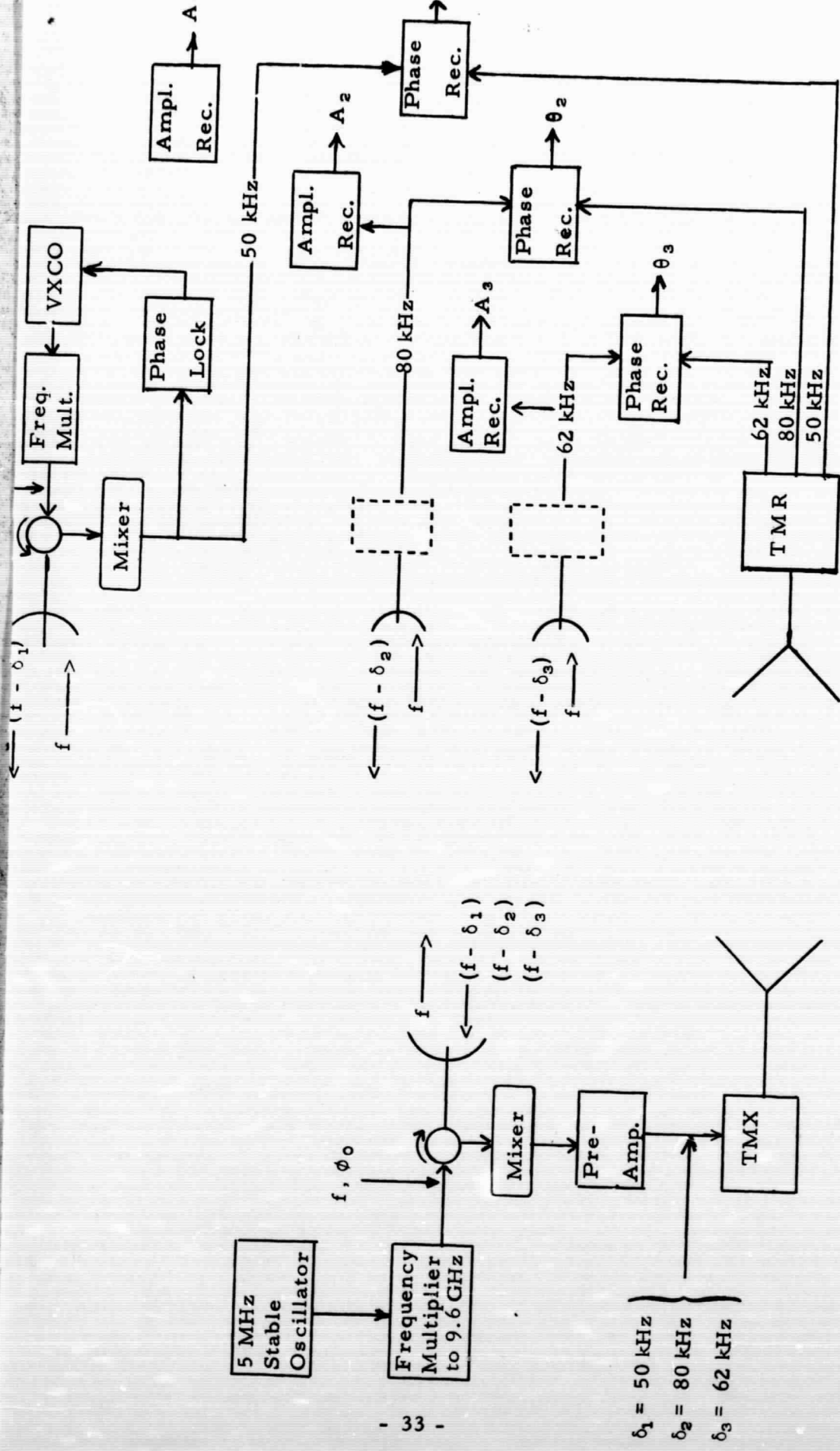
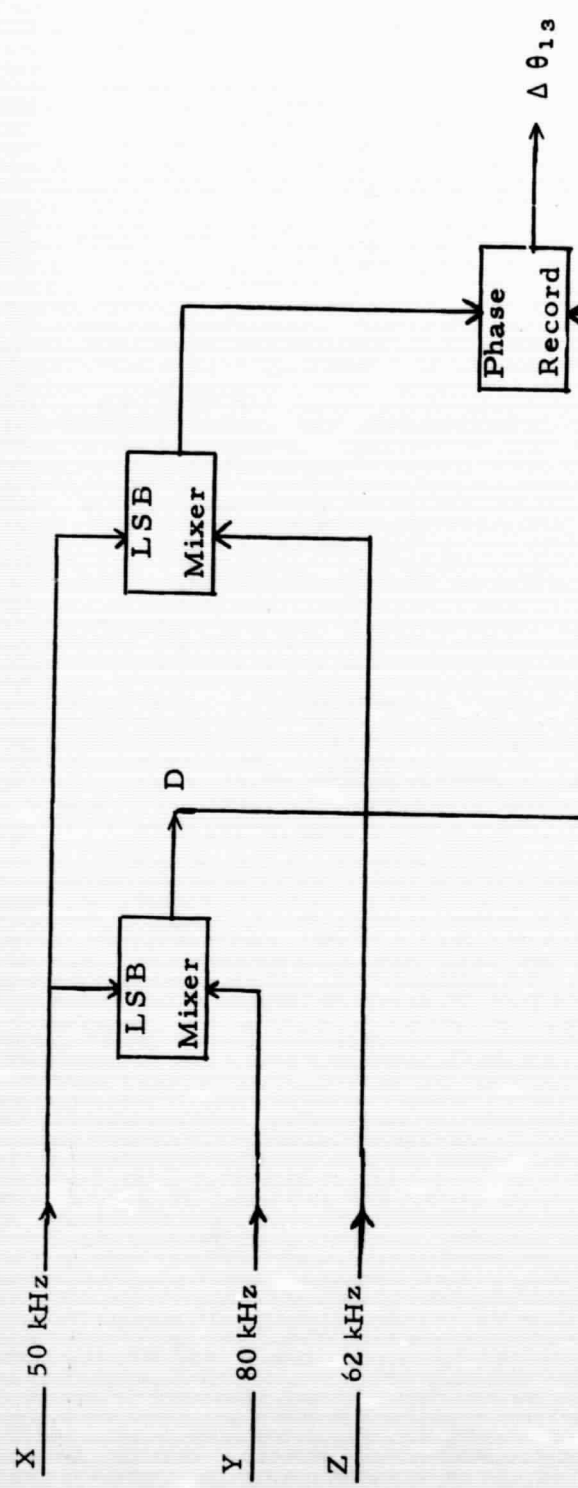


Figure 1. Phase and amplitude measurement system.

RIGHT-HAND TERMINAL - Fig. 1



REMOTE IF SIGNALS FROM  
LEFT-HAND TERMINAL - Fig. 1

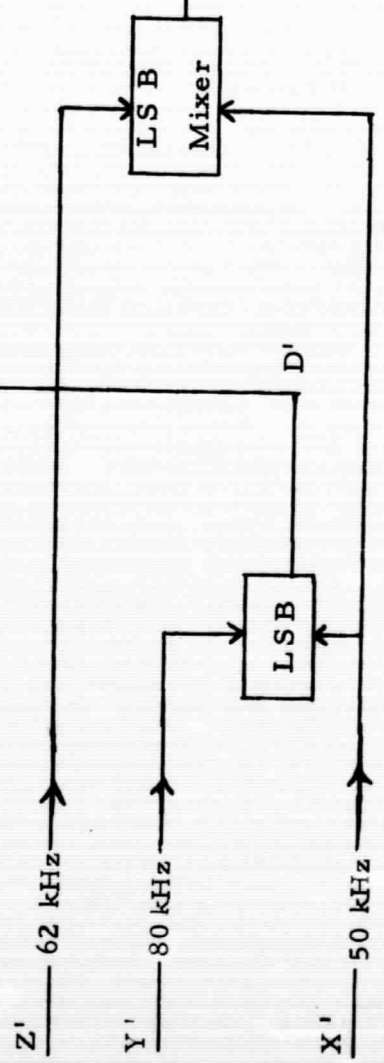


Figure 2. Phase-difference measurement system.